

A Hybrid Tracking Proposal on BESIII



Yuxi Pan (USTC)

April.21st,2009 IHEP



Outline

- 1.Motivation
- 2.Hybrid tracking concept
- 3.Simulation procedure and results
- 4.Conclusion and outlook



Motivation

- 1. Silicon vertex detectors have been widely used in HEP experiments with E_{cms} well above BEPCII energy: accurate tracking near IP, secondary vertex reconstruction...
- 2. When E_{cms} is reduced, multiple scattering dominates: distortion of track shape. Materials near IP is a disadvantage...e.g. from CLEOIII->CLEO-c
- 3. Can we coordinate the pros and cons of silicon detector to make it available for BESIII tracking?
- 4. For my own study purpose, get to know the offline analysis framework of HEP experiment such as BESIII



Before Hybrid tracking...

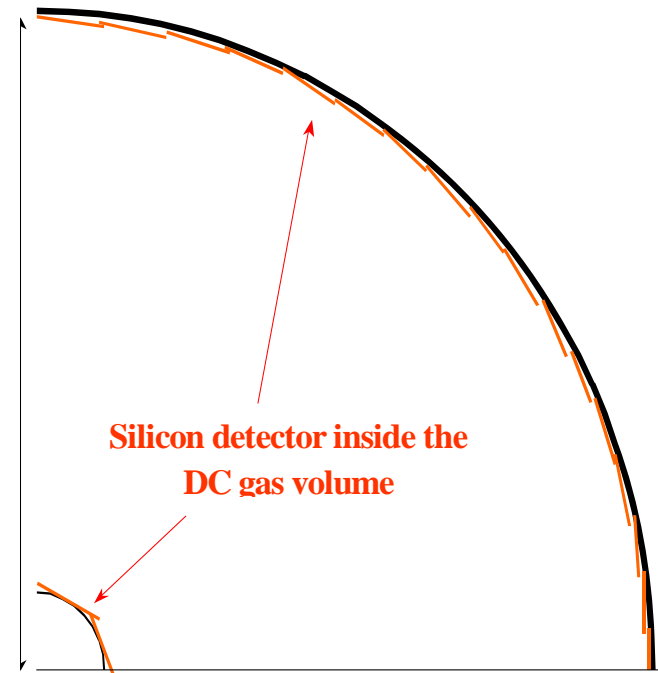
Current MDC performance:

1. Single wire resolution: $< 130 \mu\text{m}$
2. σ_p/p for 90° tracks @ 1 GeV and 1 T $\sim 0.5\%$
3. $\sigma(dE/dx)$ $6\sim 7\%$ π/K 700 MeV/c
4. π/K separation by dE/dx up to 0.77 GeV/c

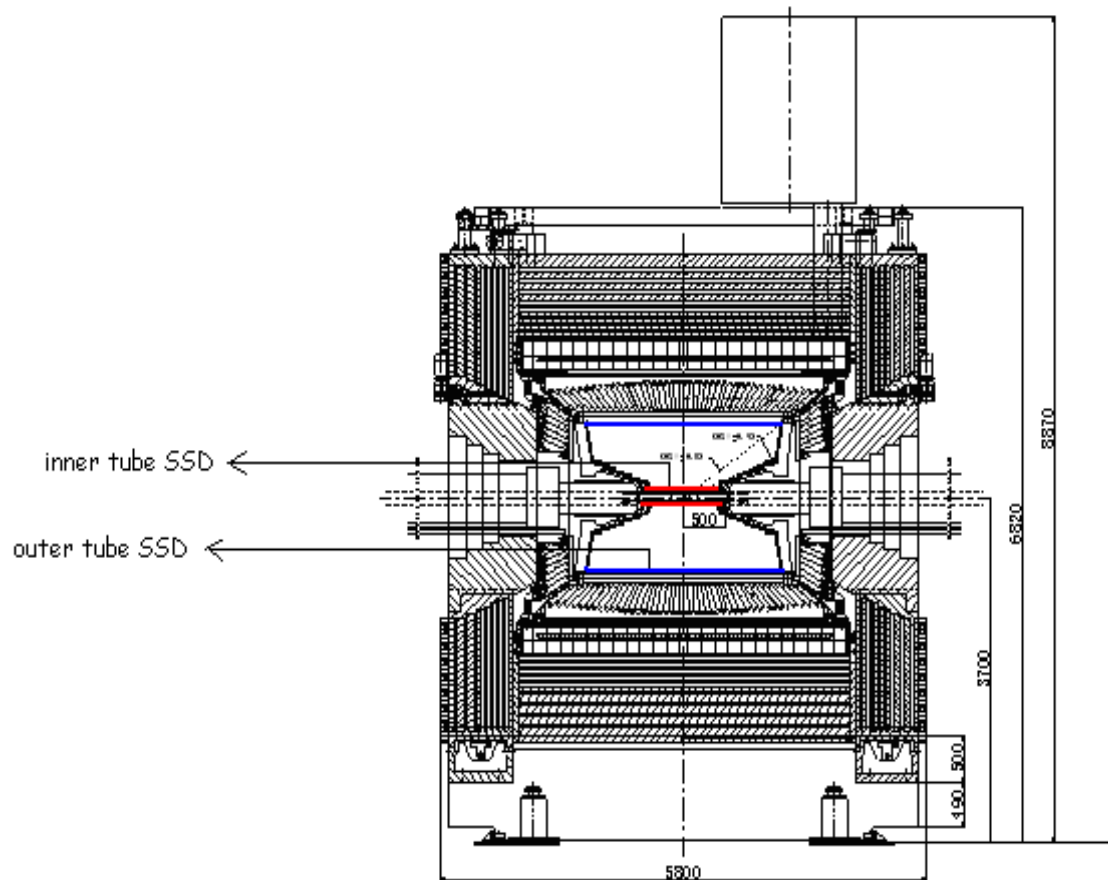
Hybrid tracking concept : overview

--by Prof.Zhao Tianchi

- 1. Hybrid tracking design to improve momentum resolution (SSD+MDC)
- 2. Low production threshold of e-/ion pair allows more precise dE/dX measurement
- 3. Need to deal with multiple scattering->on p direction



SSD in BESIII





Hybrid tracking: SSD performance

1. Configuration of Silicon Micro-Strip Detector:

Strip pitch: $D = 50 \mu\text{m}$

Single layer position resolution: $\sigma = 7 \sim 8 \mu\text{m}$ (MDC wire resolution $130 \mu\text{m}$)

Typical silicon thickness: $300 - 500 \mu\text{m}$ ($0.15 - 0.25 X_0$)

2. dE/dX :

production of e^-/ion pair in He- C_3H_8 gas is $\sim 60/\text{cm}$

In silicon, production of e^-/hole pair is $80/\mu\text{m}$

40,000 e^-/hole pairs in one layer of $500 \mu\text{m}$ silicon detector

4,000 ions all through MDC track ($\sim 0.7\text{m}$)



Hybrid tracking: advantage

multiple scattering...

Silicon thickness: 300 - 500 μm (0.15 - 0.25 X_0)

The material of the 43 layers of MDC is only 0.29% X_0

(~0.72m long track)

$$\frac{\sigma_{P_t}}{P_t}_{MS} = \frac{0.05}{BL} \times \frac{1}{\beta} \times \sqrt{1.43 \frac{L}{X_0} \left[1 + 0.038 \ln \frac{L}{X_0}\right]}$$

Significant influence especially on low momentum tracking

->advantage of hybrid tracking approach: track shape will not be distorted by silicon layers, other than traditional silicon vertex trackers with multi-layer complex



Simulation objectives:

- 1.To test whether(or how much) momentum resolution can be improved if we have two (nearly) fixed hit point at inner and outer tube of MDC?
- 2.influence of multiple scattering(on **p direction**)



Simulation procedure and results

- 1. Detector definition
- 2. Track reconstruction:
 - a. joint track reconstruction based on Kalman Filter
 - b. modified MDC layers for the purpose of using MdcPatRec
- 3. Effects of multiple scattering



1. Detector definition

A. simple silicon cylinder fixed on the wall of beam pipe

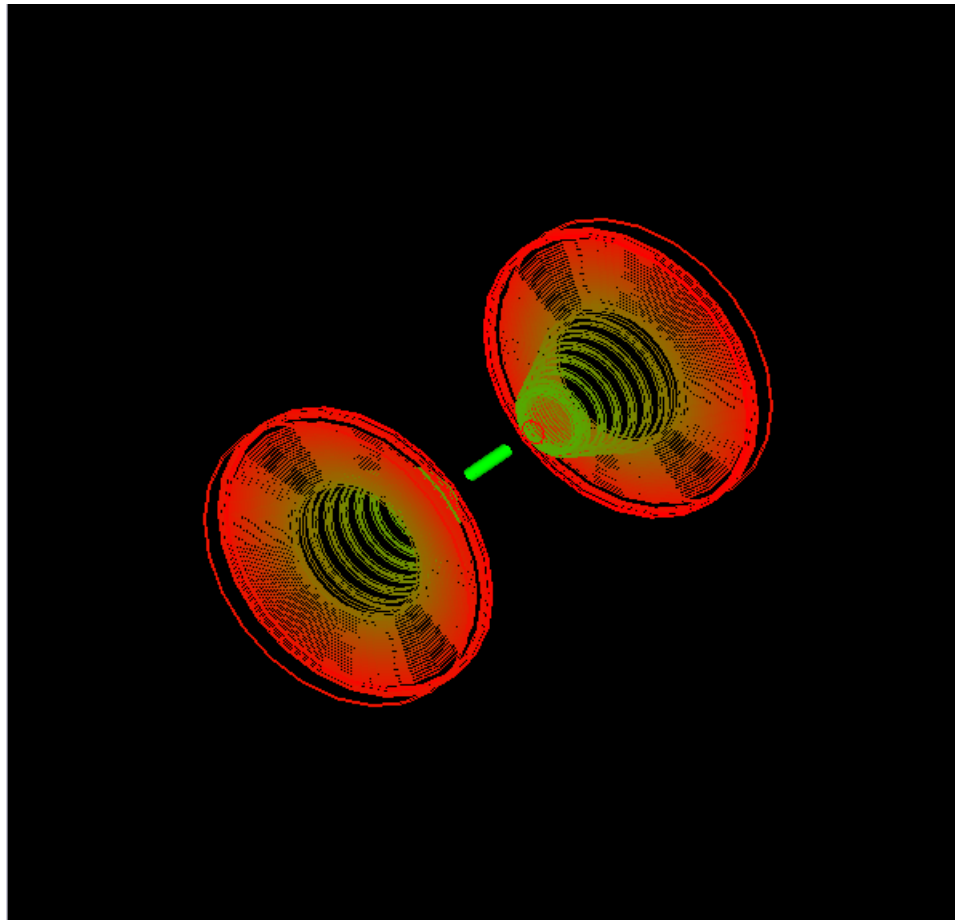
B. length: 300mm

thickness: 500 μ m

C. record hit position and energy deposit

no smear to hit position

Detector geometry:





2. Track reconstruction

A. Joint track reconstruction based on Kalman Filter --BOSS 6.3.1

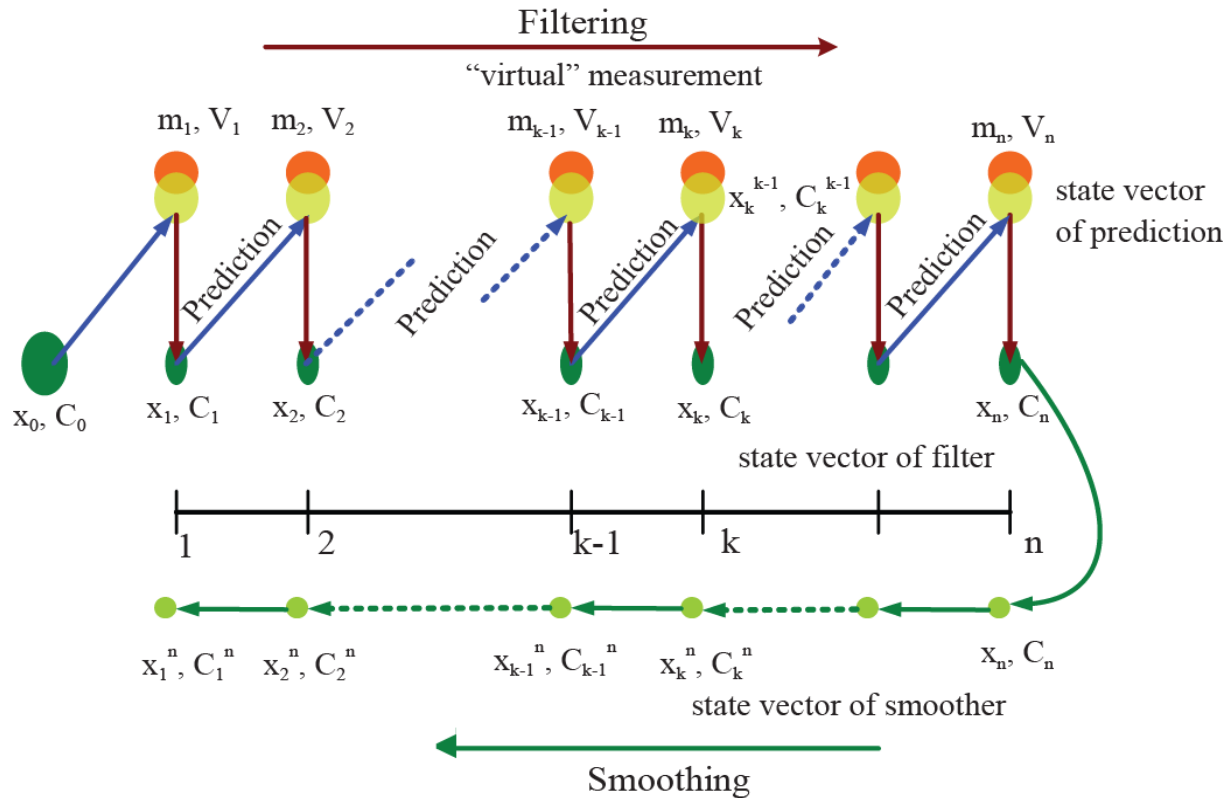
Kalman Filter: a recursive solution to the discrete-data linear(or nonlinear) filtering problem;
widely used in track and vertex fitting

common process:

predict->filter->smooth.

Kalman Filter

Common process:





Kalman Filter

- Track fitting with hits on silicon detector combined:

5 track parameters represent state vector:

$$X_k = \{d_0, \phi_0, \kappa, dz, \tan \lambda\}^T$$

X_k uniquely describes an helix



Joint track fitting

- Add hits on inner silicon detector to Kalman routine:

state prediction: $X_k^- = X_{k-1}$ (from MDC)

$$P_k^- = P_{k-1} + Q$$

measurement: $Z_k = H_K X_K + V_K$ V_K : noise

define $H_k = \{0, 0, 1, 0, 0\}$ measurement matrix;
use κ to be the measurement quantity;

$$\kappa = 1/Pt$$



Joint track fitting

Calculate residual:

$$\text{Residual} = \kappa_{\text{mea}} - \kappa_{\text{pre}}$$

where κ_{mea} is from:

$$\kappa_{\text{mea}} = 1/pt_{\text{mea}}; \quad pt_{\text{mea}} = 0.3BR_{\text{mea}};$$

R_{mea} = distance(hit position on silicon detector-circle center) \rightarrow using 90deg outgoing tracks



Joint track fitting

- Calculate circle center:

$$X_0 = (R_{\text{pre}} - d_0) \cos(\phi_0)$$

$$Y_0 = (R_{\text{pre}} - d_0) \sin(\phi_0)$$

Feedback residual to update state vector by Kalman gain coefficient: K_k

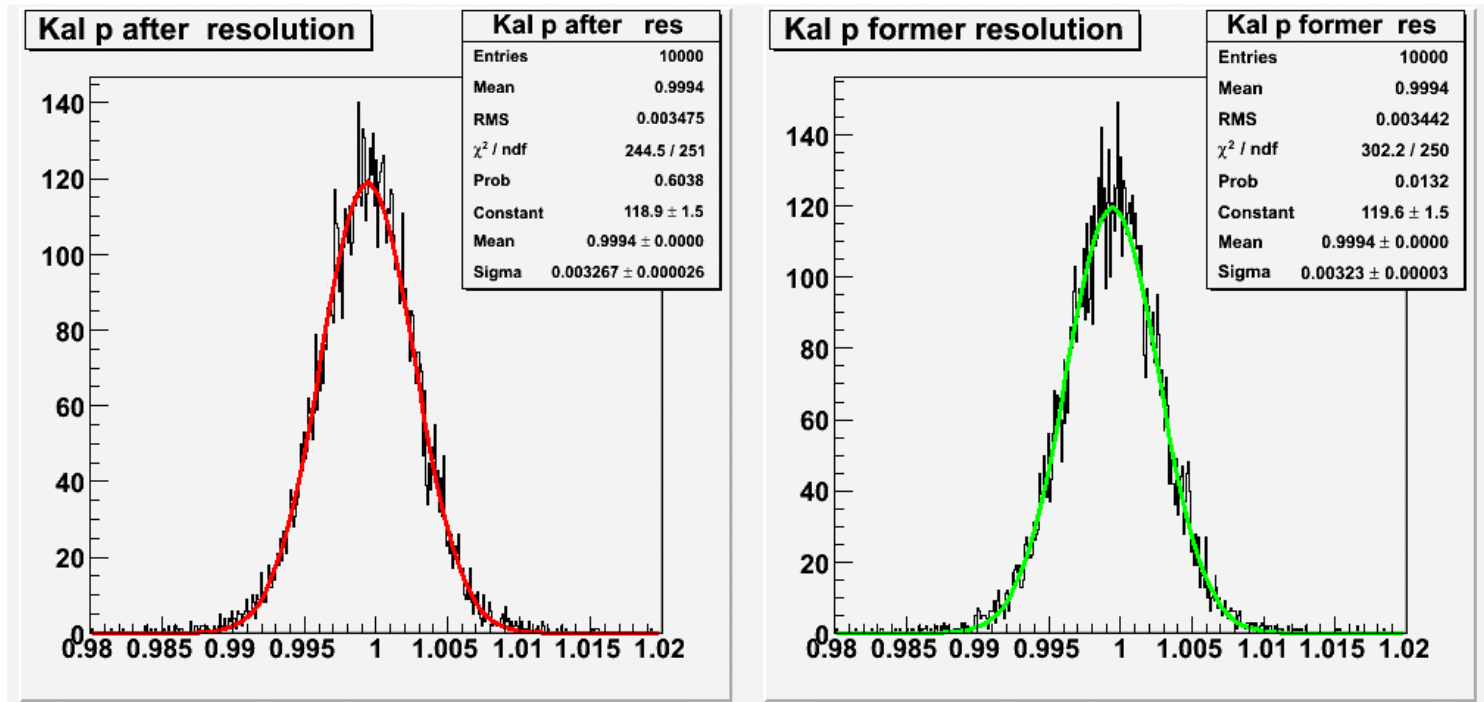
$$K_k = P_k^{-1} H^T (H P_k^{-1} H^T + R)^{-1} \quad (R: \text{covariance of measurement noise})$$

$$X_k = X_k^- + K_k (Z_k - H_k X_k^-)$$

Joint track fitting

- Retrieve updated track parameter κ

Pt statistics: 1 GeV muon-, theta=90deg





Joint track fitting

- Result:

momentum resolution before silicon detector was added: 0.323%

after: 0.327%

no significant change

maybe due to the insensitivity of measurement quantity



Joint track fitting

- Further improvement of this algorithm:
use BESIII original definition of
measurement matrix and state prediction
equation;



2. Track reconstruction

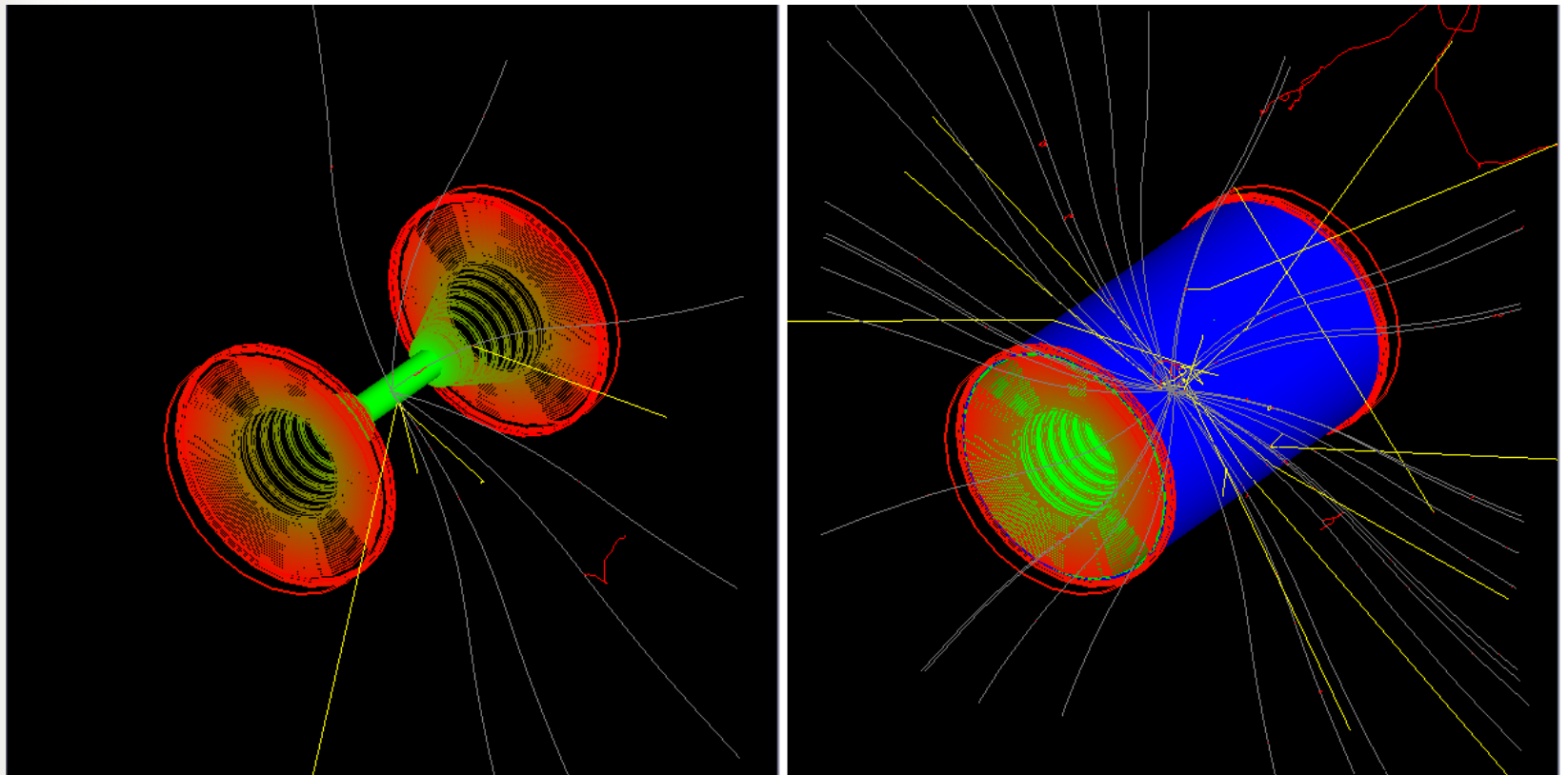
B. Modified MDC layers for the purpose of using MdcPatRec:

--BOSS 6.4.1

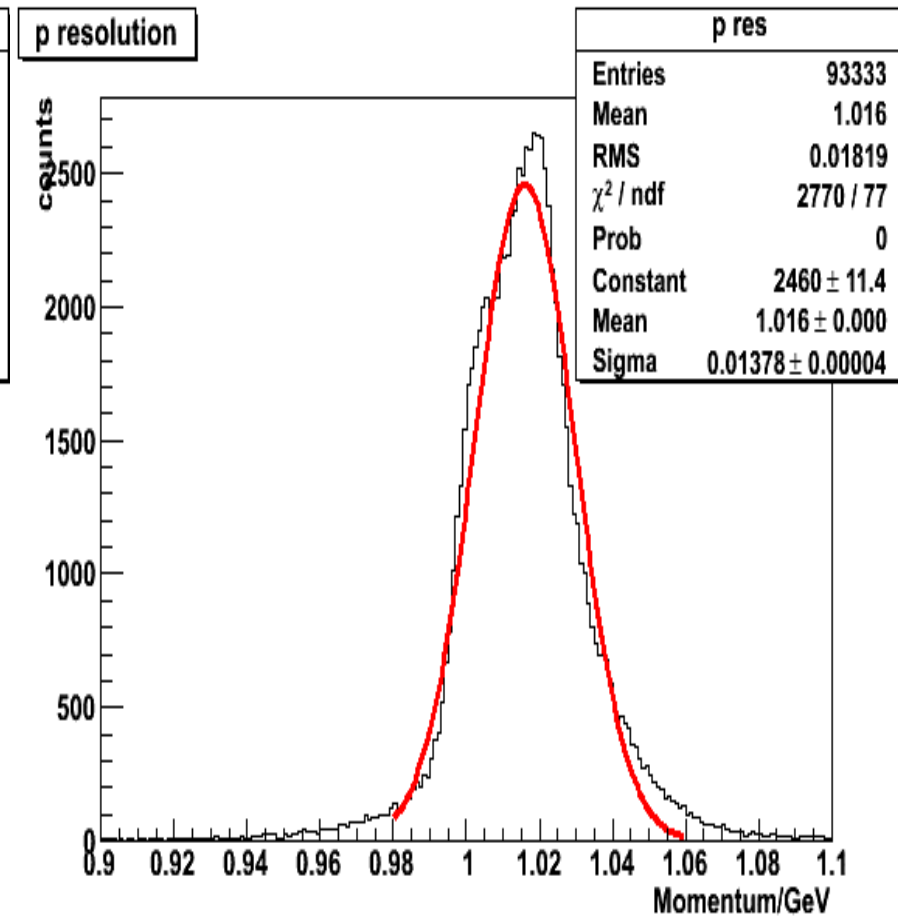
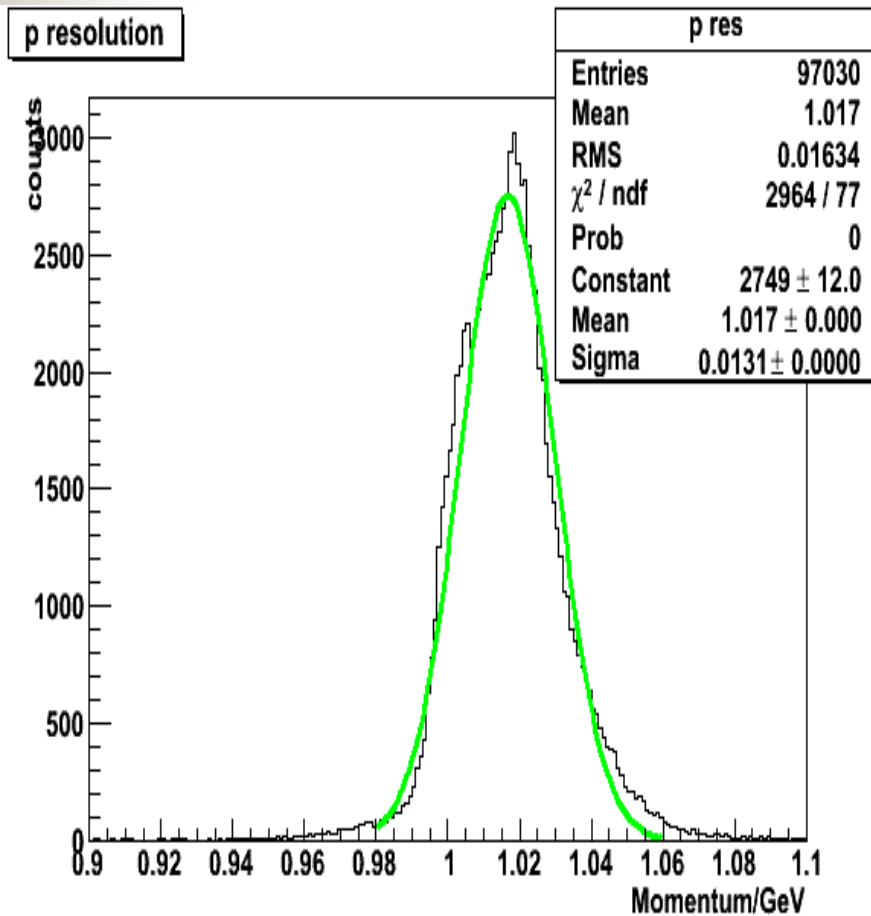
1. Change the materials of 1/43 MDC layers to silicon
2. Spatial resolution of these two layers are set to be 10um

So we can use MdcRecPat algorithm to reconstruct charged tracks without too much modification of the code

Detector geometry:



Momentum resolution





Momentum resolution

- 1.no silicon layers
- 2. double gaussian spatial resolution in digitization (from Calib Func)

p resolution: 1.31%

1GeV u- with even $\cos(\theta)$ distribution

- 1.1/43 silicon layers with fixed resolution 10um
- 2.other layers adopt double gaussian

p resolution: 1.38%

But the unsatisfying χ^2/ndf renders the result trustless...maybe due to the limitation of MdcPatRec



Momentum resolution

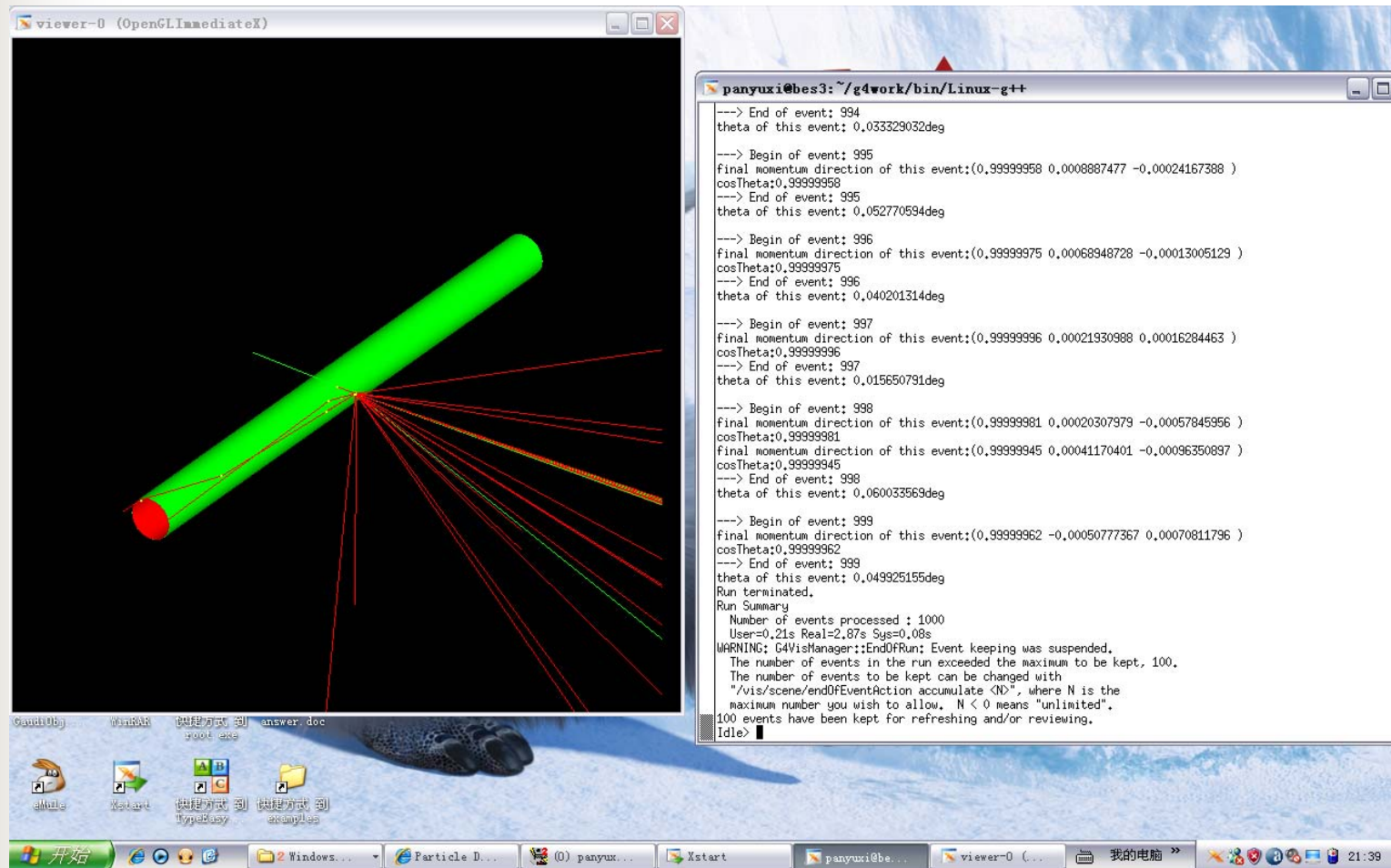
- A better way to obtain the momentum resolution might be achieved if we can modify the definition of materials in **KalFitAlg**



3. Effects of multiple scattering

- 1. estimate the influence of multiple scattering after SSD been adopted → **change of P direction;**
- 2. energy deposit during particles penetrating SSD → the influence on **P magnitude;**

Simulation process



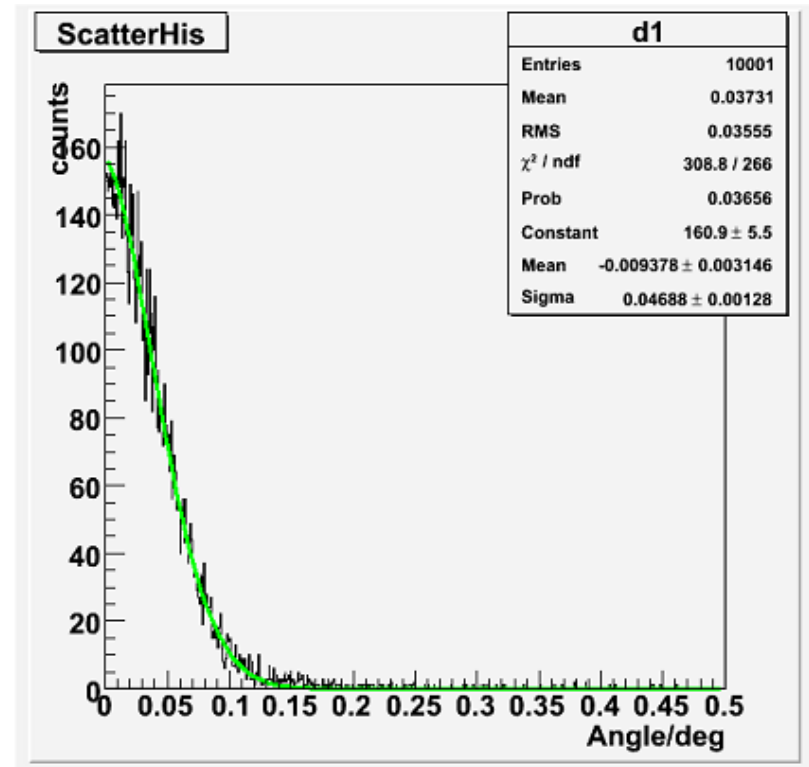
The screenshot displays a Linux desktop environment with a blue sky background. In the foreground, there are two windows:

- viewer-0 (OpenGLImmediateX):** A 3D visualization window showing a bright green cylinder. From one end of the cylinder, several red lines radiate outwards, representing particle tracks or simulation results. A green arrow points towards the cylinder.
- Terminal Window:** A terminal window titled "panyuxi@bes3: ~/g4work/bin/Linux-g++" showing the output of a simulation. The output includes event details such as event numbers (994-999), theta values, and final momentum directions. The simulation ends with a "Run terminated" message and a "Run Summary" indicating 1000 events were processed. A warning message states: "WARNING: G4VisManager::EndOfRun: Event keeping was suspended. The number of events in the run exceeded the maximum to be kept, 100. The number of events to be kept can be changed with "/vis/scene/endOfEventAction accumulate <N>", where N is the maximum number you wish to allow. N < 0 means "unlimited". 100 events have been kept for refreshing and/or reviewing. Idle>".

The desktop environment includes a taskbar at the bottom with icons for "开始" (Start), "eMule", "Xstart", "Type4asy", and "examples". The system tray shows the time as 21:39.

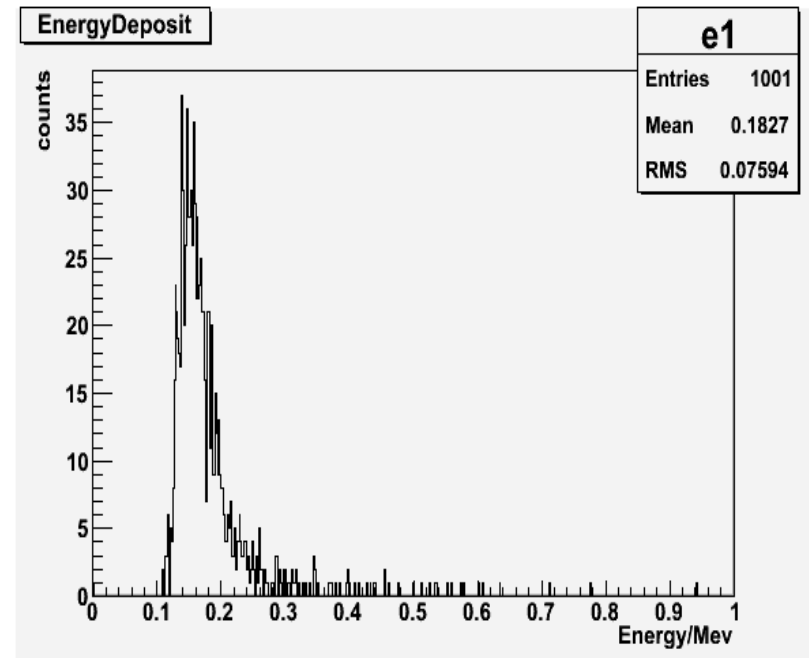
Simulation result: Scattering angle

- 1. 1GeV electron
- 2. 1000 events;
- 3. mean value 0.037°
 $\sim 0.02^\circ$ from
theoretical prediction
- 4. need to estimate
this influence on
vertex location after
track extrapolation



Simulation result: energy deposit

- 1. 1GeV electron
- 2. 1000 events;
- 3. Mean value:0.18MeV
~insignificant
influence on p magnitude
- 4. Approximately Landau
shape





Conclusion and outlook

- Conclusion:

1. Silicon detector has been added to BESIII detector definition;
2. Calculate momentum resolution by joint track fitting and MdcPatRec: no significant improvement had been seen;
3. Simulate the influence of inner silicon layers on particle's momentum



Conclusion and outlook

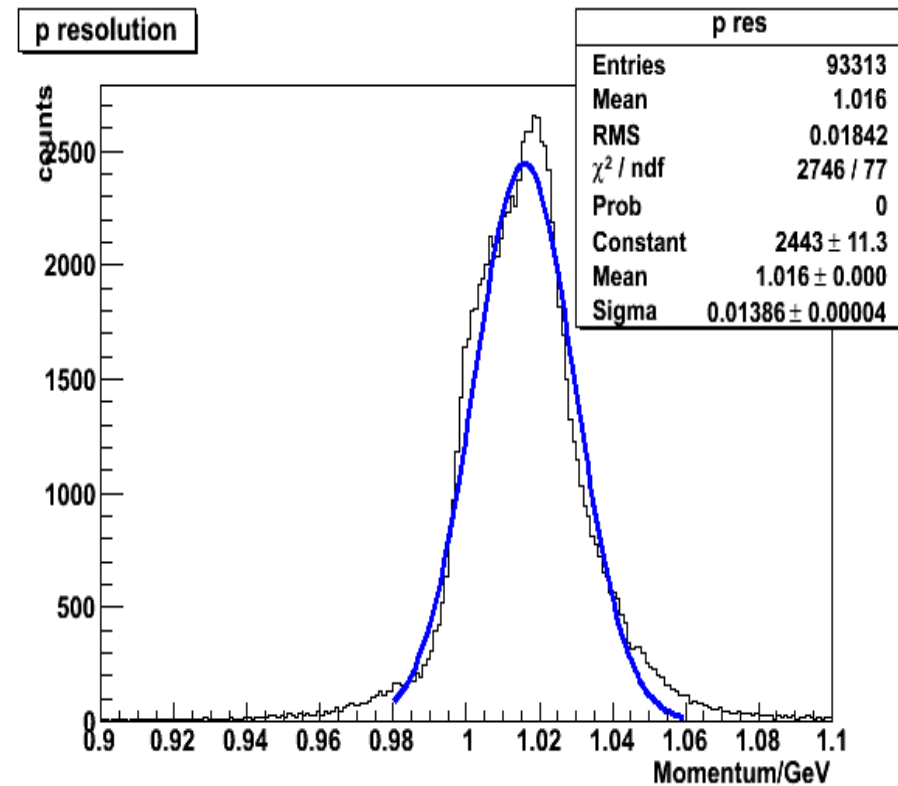
- Outlook:



Both track reconstruction method need to be refined: hope this work could be done by me or someone else under guidance of a specialist from IHEP

Thank you!!



- 3. No silicon layers but reduce 1/43 spatial resolution to 10 μm
p resolution 1.39%




$$\left(\frac{\sigma_{pt}}{p_t}\right)_{pos} = \frac{3.3 \times 10^2 \times \sigma_x}{B \times L^2} \times p_t \times \sqrt{\frac{720}{n+5}}$$



Change the fitting weight in MdcPatRec

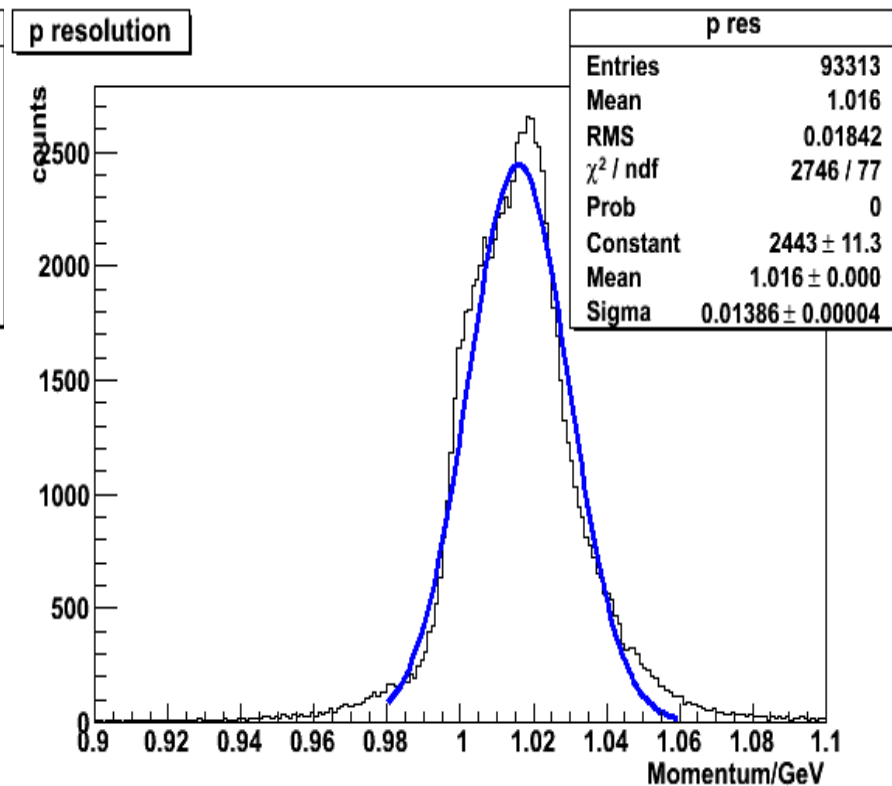
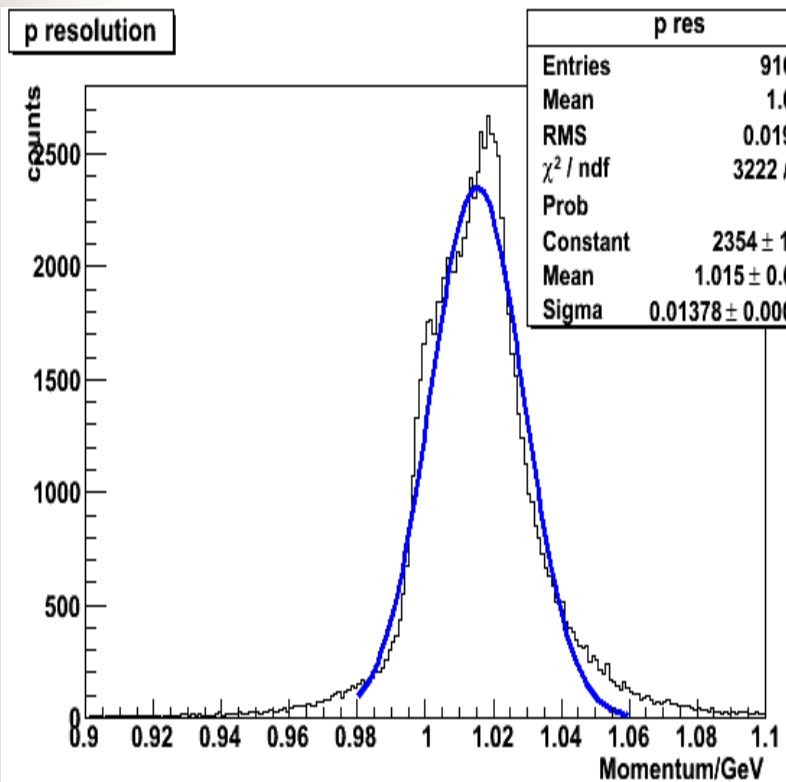
- When LayerNo=1 or 43

MdcHit->sigma=10um

others retrieved from CalibFunSvc

$$\text{Chi}^2 = \sum_i \frac{\text{drift}_i - \text{doca}_i}{\text{sigma}_i} \quad \text{weight} = 1/\text{sigma}$$

Result





Result

- 1. No silicon layers but 1/43 spatial resolution change to 10 um

weight with **new** layer resolution

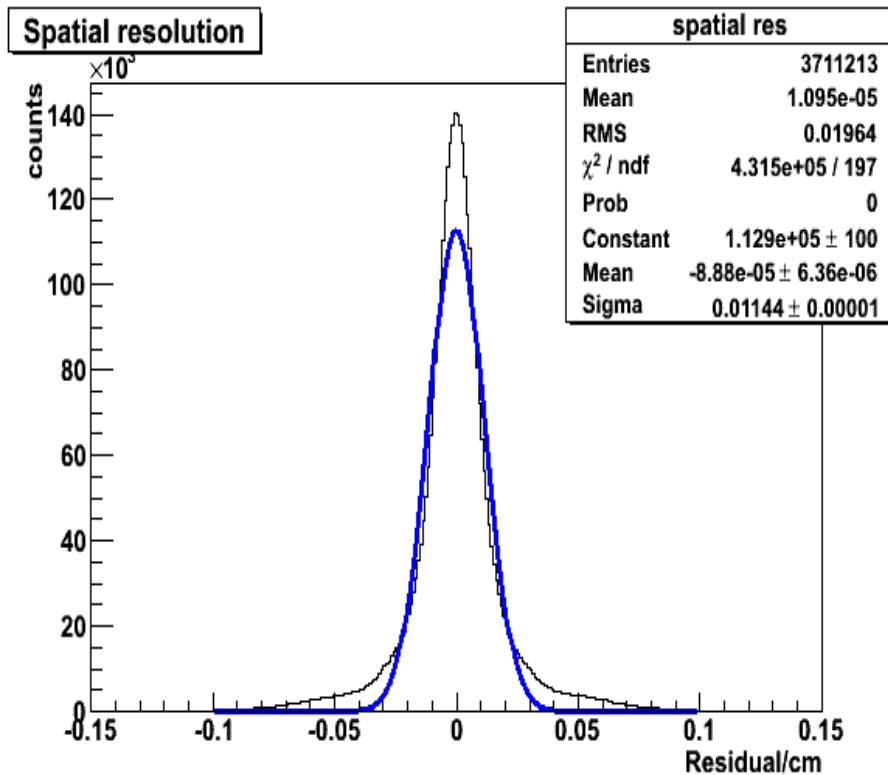
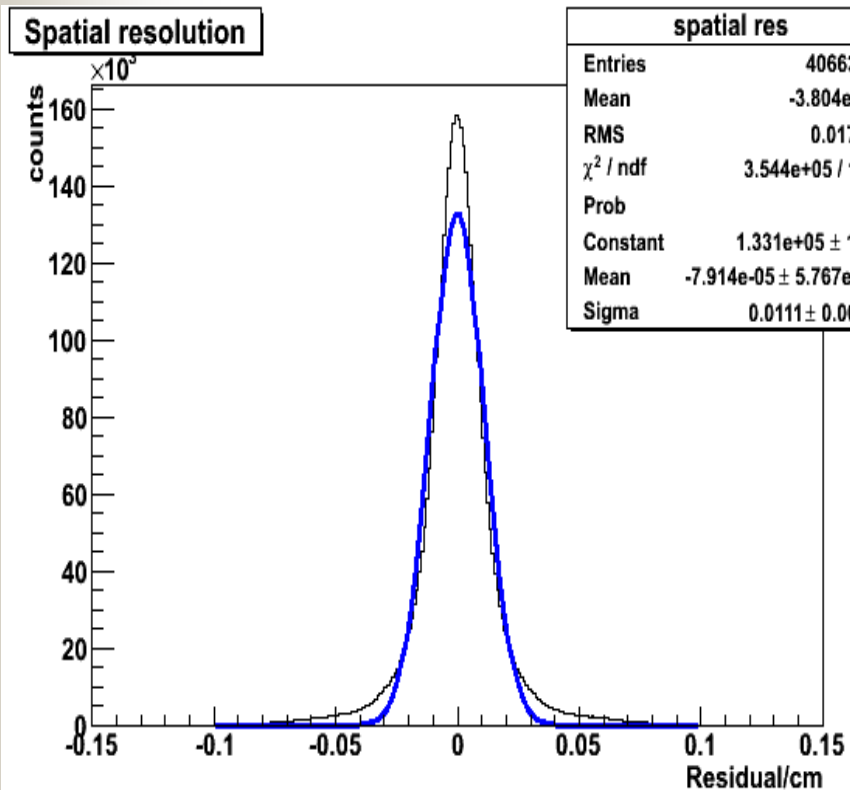
1.378%

- 2. No silicon layers but 1/43 spatial resolution change to 10 um

weight with **previous** Mdc layer resolution

1.386%

Wire resolution: all layers



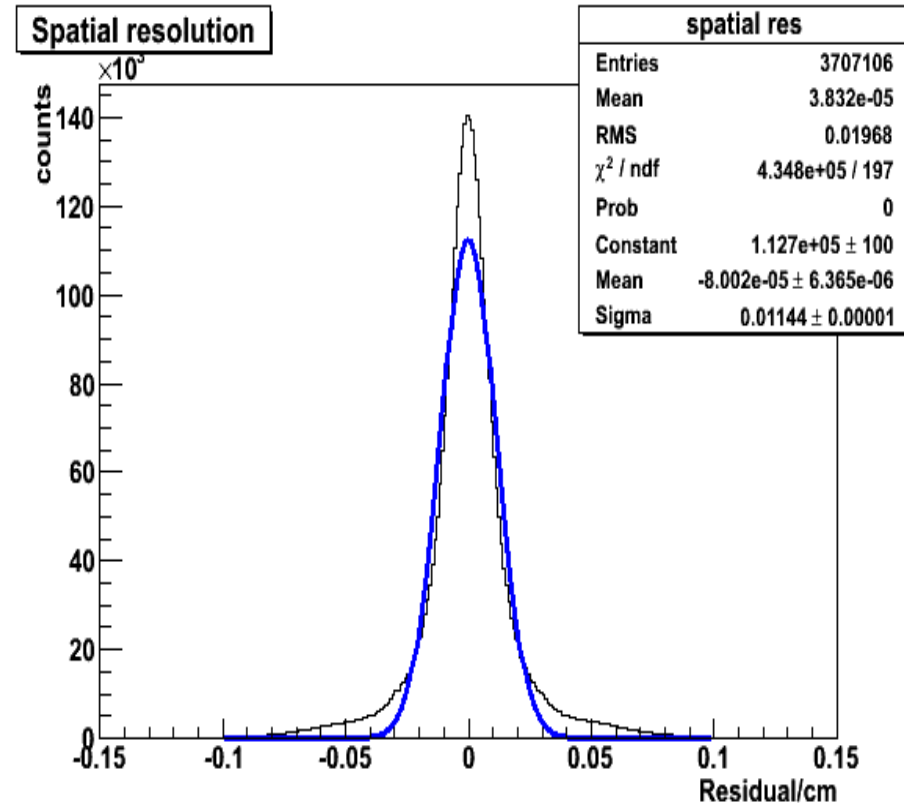
■ No silicon layers: **111um**

■ With 1/43 silicon layers: **114um**

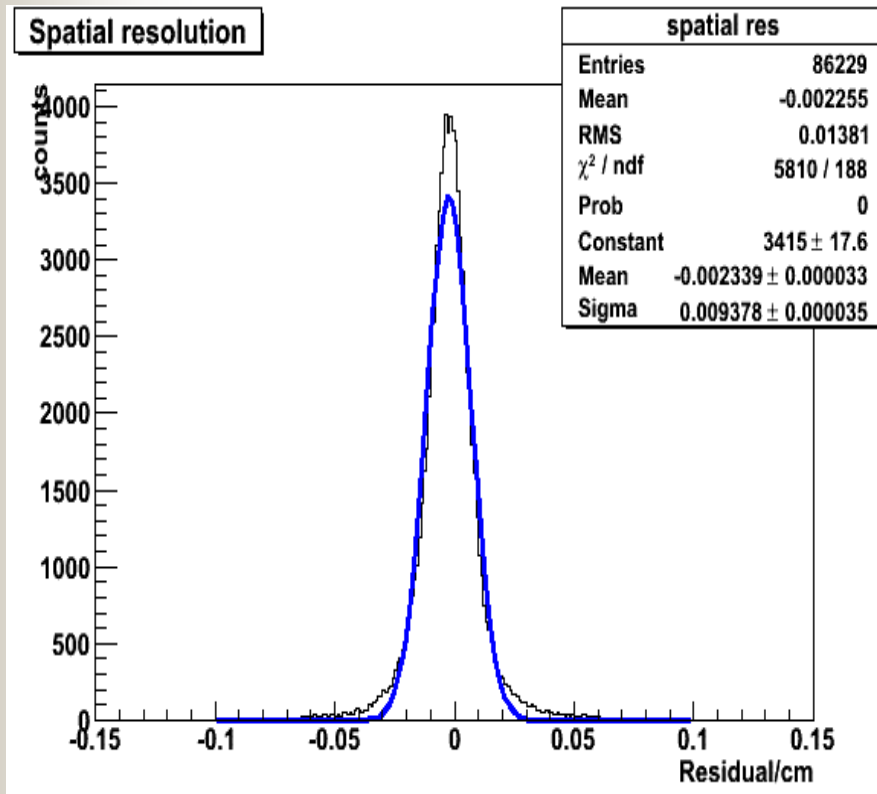
Wire resolution: all layers

- No silicon layers but with reduced spatial resolution of 1/43 layers

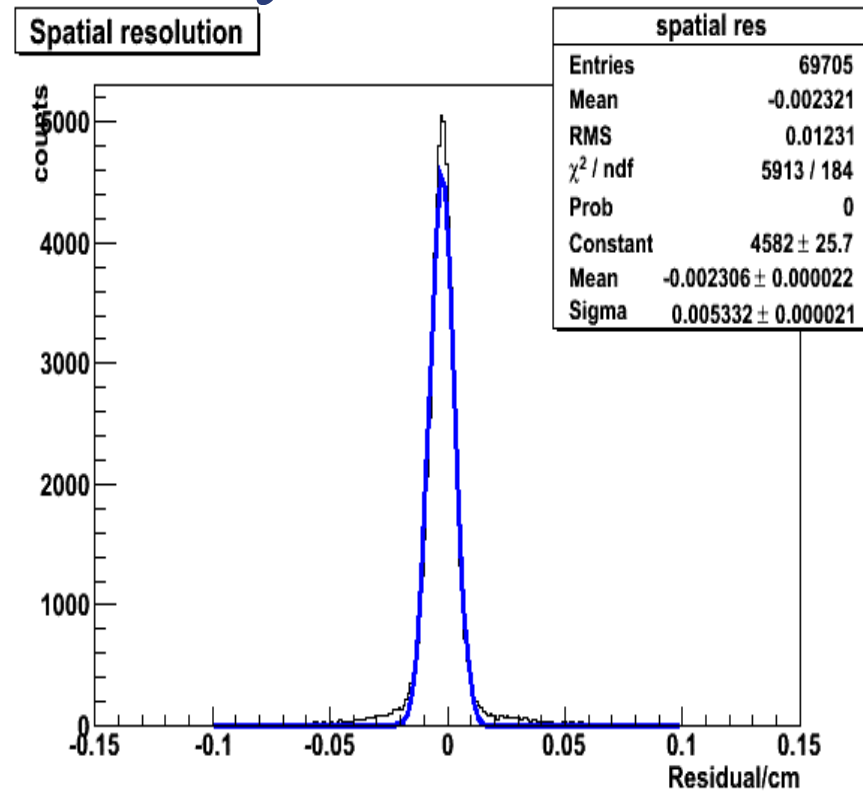
114 μ m



Wire resolution: first layer



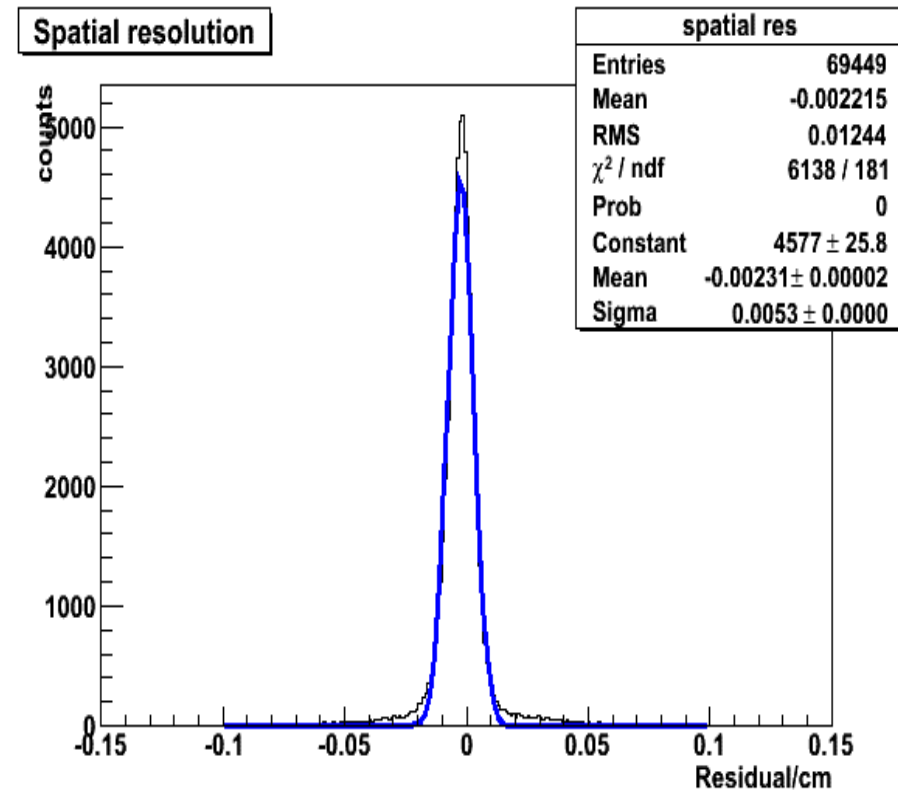
No silicon layers : **94 um**



With 1/43 silicon layers
53um

Wire resolution: first layer

No silicon layers but
reduced 1/43 spatial
resolution: **53um**



Outlook: Shifted inner SSD layers

- In gaps between inner tube and inner SSD, several layers of sense wire will determine the momentum direction before scattered by SSD layers
- Simulation is still in need

